PMRF-ISSS Teaching Programme Prime Minister Research Fellowship students' teaching requirement facilitated by the Institute of Smart Structures and Systems



# Module PMRF-ISSS033/2023 Introduction to Elliptic curves and Modular forms

## Name of the PMRF student

# Ajay Prajapati

**Required background of the students taught** Mathematics, Computer Science Pre-requisites: Basic Abstract Algebra, Basic Complex Analysis

### **Online session coordinator**

Will be chosen from the list of registrants



Graphic relevant to the module

## Details of the content of the module

- **Introduction to the Congruent Number** problem and its relation to elliptic curves: Congruent number problem is a 2000-year-old problem about numbers which can be obtained as area of a right-angled triangle. This problem is related to elliptic curves which are modern (19<sup>th</sup> century) objects.
- **Elliptic Curves:** These are curves defined by non-singular cubic equations. Then we will study doubly-periodic functions and show that an elliptic curve over C is a torus.
- Hasse-Weil L-function of an Elliptic Curve: This is an analytic object defined using arithmetic information of the curve.
- Modular Forms: These are functions on upperhalf plane satisfying certain symmetry properties and turn out to be highly useful in number theory.
- **References:** "Introduction to Elliptic curves and Modular forms" by Neal Koblitz.

### Schedule of the module

- Live lectures on Tuesdays (4:30 PM to 6:30 PM)
- In unforeseen situations, recorded lectures will be uploaded by 6:30 PM on Tuesdays.
- Starts- 12<sup>th</sup> September 2023
- Ends- 5th December 2023

### Meeting link : Will be shared later

### Link

### Contact email ID: isss.forum@gmail.com

**Registration link:** 

https://docs.google.com/forms/d/e/1FAIp QLSexjIgZTyrirZG524lw8K MUtFPzJ9pDdY YwZ0HGgT6zvhVmg/viewform?usp=pp\_url